# FACULTY OF EDUCATION <br> Department of <br> Curriculum and Pedagogy 

# Mathematics Number: Percents 

## Science and Mathematics Education Research Group

## Shopping with Percents



## Shopping with Percents I

25\% increase

## \$ 400



## \$ ???

A local computer store receives its stock for $\$ 400$ per computer. The store marks up this price by $25 \%$. What is the listed price of the computer before tax?
A. \$ 100
B. \$ 425
C. $\$ 450$
D. \$ 475
E. \$ 500

## Solution

## Answer: E

Justification: A 25\% increase means an additional 0.25 times the original price must be paid.

$$
\$ 400+(\$ 400 \times 0.25)=\$ 400+\$ 100=\$ 500
$$

A $25 \%$ percent increase also means the same as paying $125 \%$ of the original price.

$$
\$ 400 \times 1.25=\$ 500
$$

Note that a $25 \%$ increase does not mean you only pay $25 \%$ the original price.

## Shopping with Percents II

Two computer stores each have a promotion on their computers.
Best Purchase: 10\% off all computers today!
Future Store: You pay $90 \%$ of the price, we'll pay the rest!
If the computer you want to purchase has the same listed price in both stores, where should you buy your computer?
A. Best Purchase
B. Future Store
C. The price will be the same in both stores

## Solution

## Answer: C

Justification: A 10\% off sale is the same as only paying for $90 \%$. Consider a computer that costs $\$ 100$.

Best Purchase:

$$
\begin{aligned}
& 10 \% \text { of } \$ 100=\$ 10 \\
& (10 \% \text { off } \$ 100)=\$ 100-(10 \% \text { of } \$ 100)=\$ 90
\end{aligned}
$$

Future Store:

$$
90 \% \text { of } \$ 100=\$ 100 \times 0.90=\$ 90
$$

## Shopping with Percents III



Kevin wants to buy the computer listed for $\$ 500$. The computer happens to be on sale for $10 \%$ off. After the discount, the price is increased by $10 \%$ due to tax. The final amount that Kevin has to pay will be:
A. Greater than $\$ 500$
B. Equal to $\$ 500$
C. Less than $\$ 500$

## Solution

## Answer: C

Justification: A 10\% discount on \$500 means Kevin only pays for $90 \%$ of $\$ 500$.

$$
0.90 \times \$ 500=\$ 450 \text { (decrease of } \$ 50 \text { ) }
$$

A 10\% tax increase means Kevin plays for 110\% of the discounted price.
$1.10 \times \$ 450=\$ 495$ (increase of $\$ 45$ )
The $10 \%$ discount was applied to $\$ 500$ while the $10 \%$ increase was applied to $\$ 450$.

## Shopping with Percents IV



In the previous question, Kevin paid $\$ 495$ on an item that was first discounted by $10 \%$, followed by a tax increase of $10 \%$.

If the $\$ 500$ item was first increased $10 \%$ by tax, followed by a $10 \%$ discount, the final price Kevin has to pay will be:
A. Greater than $\$ 495$
B. Equal to $\$ 495$
C. Less than $\$ 495$

## Solution

## Answer: B

Justification: The amount Kevin has to pay will be exactly the same. Note:
$0.90 \times \$ 500=\$ 450$ (decrease of $\$ 50$ )
$1.10 \times \$ 450=\$ 495$ (increase of $\$ 45$ )
is the same as
$1.10 \times \$ 500=\$ 550$ (increase of $\$ 50$ )
$0.90 \times \$ 550=\$ 495$ (decrease of $\$ 55$ )

## Shopping with Percents V



If an item's price is increased by $10 \%$ then decreased by $10 \%$ (or decreased first and then increased), what percent of the original do you have to pay for?
A. $90 \%$
B. $99 \%$
C. 100\%
D. 101\%
E. 110\%

## Solution

## Answer: B

Justification: Assume an item costs \$100. For a 10\% increase you multiply the cost by 1.1. For a $10 \%$ decrease you multiply the cost by 0.9 .

$$
\$ 100 \times 1.1 \times 0.9=\$ 100 \times 0.9 \times 1.1=\$ 99
$$

Therefore you actually pay for $99 \%$ of the original price.

