a place of mind

## Mathematics <br> Shape and Space: Polygon Angles

## Science and Mathematics Education Research Group

## Polygon Angles



## Polygon Angles I

What is the sum of all internal angles in this equilateral triangle?
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: B

Justification: The sum of all internal angles in an equilateral triangle is $180^{\circ}$.

## Polygon Angles II

What is the internal angle of this equilateral triangle?
A. $30^{\circ}$
B. $60^{\circ}$
C. $90^{\circ}$
D. $180^{\circ}$
E. No idea


## Solution

## Answer: B

Justification: The sum of all internal angles is $180^{\circ}$, and the triangle has three corners, so $180 / 3=60^{\circ}$.

## Polygon Angles III

What is the external angle of this equilateral triangle?
A. $30^{\circ}$
B. $60^{\circ}$
C. $90^{\circ}$
D. $120^{\circ}$
E. $180^{\circ}$


## Solution

## Answer: D

Justification: The internal angle and external angle add up to $180^{\circ}$ because they share a straight line.

## Polygon Angles IV

What is the sum of all external angles in this equilateral triangle?
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: B

Justification: The sum of all external angles in an equilateral triangle is $3 \times 120=360^{\circ}$.

## Polygon Angles V

What is the internal angle of this square?
A. $30^{\circ}$
B. $60^{\circ}$
C. $90^{\circ}$
D. $180^{\circ}$
E. No idea


## Solution

## Answer: C

Justification: Squares have perpendicular sides and bases, which have a right angle of $90^{\circ}$.

## Polygon Angles VI

What is the sum of all internal angles in this square?
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all internal angles in an square is $4 \times 90=360^{\circ}$.

## Polygon Angles VII

What is the external angle of this square?
A. $30^{\circ}$
B. $60^{\circ}$
C. $90^{\circ}$
D. $120^{\circ}$
E. $180^{\circ}$


## Solution

## Answer: C

Justification: The internal angle and external angle add up to $180^{\circ}$ because they share a straight line.

## Polygon Angles VIII

What is the sum of all external angles in this square?


## Solution

## Answer: D

Justification: The sum of all external angles in a square is $4 \times 90=360^{\circ}$.

## Polygon Angles IX

What is the sum of all internal angles in this regular pentagon?
A. $180^{\circ}$
B. $360^{\circ}$
C. $540^{\circ}$
D. $720^{\circ}$
E. No idea


## Solution

## Answer: C

Justification: The sum of all internal angles in a pentagon is the same as three triangles (see picture below).


## Polygon Angles X

A. $54^{\circ}$
B. $72^{\circ}$
C. $108^{\circ}$
D. $144^{\circ}$
E. No idea

What is the internal angle of this regular pentagon?

## Solution

## Answer: C

Justification: A pentagon has 5 corners, thus each internal angle is $540 / 5=108^{\circ}$.

## Polygon Angles XI

What is the external angle of this regular pentagon?
A. $54^{\circ}$
B. $72^{\circ}$
C. $108^{\circ}$
D. $144^{\circ}$
E. No idea


## Solution

## Answer: B

Justification: The internal angle and external angle add up to $180^{\circ}$ because they share a straight line.

## Polygon Angles XII

What is the sum of all external angles in this regular pentagon?
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all external angles in a regular pentagon is $5 \times 72=360^{\circ}$.

## Polygon Angles XIII

What is the sum of all internal angles in this regular hexagon?
A. $180^{\circ}$
B. $360^{\circ}$
C. $540^{\circ}$
D. $720^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all internal angles in a hexagon is the same as four triangles (see picture below).


## Polygon Angles XIV

What is the internal angle of this regular hexagon?
A. $60^{\circ}$
B. $90^{\circ}$
C. $120^{\circ}$
D. $144^{\circ}$
E. No idea


## Solution

## Answer: C

Justification: A hexagon has 6 corners, thus each internal angle is $720 / 6=120^{\circ}$.

## Polygon Angles XV

What is the external angle of this regular hexagon?
A. $60^{\circ}$
B. $90^{\circ}$
C. $120^{\circ}$
D. $144^{\circ}$
E. No idea


## Solution

## Answer: A

Justification: The internal angle and external angle add up to $180^{\circ}$ because they share a straight line.

## Polygon Angles XVI

What is the sum of all external angles in this regular hexagon?
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all external angles in a regular hexagon is $6 \times 60=360^{\circ}$.

## Polygon Angles XVII

What is the sum of all internal angles in this regular heptagon?
A. $540^{\circ}$
B. $720^{\circ}$
C. $900^{\circ}$
D. $1080^{\circ}$
E. No idea


## Solution

## Answer: C

Justification: The sum of all internal angles in a heptagon is the same as five triangles (see picture below).


## Polygon Angles XVIII

What is the internal angle of this regular heptagon?
A. $70^{\circ}$
B. $\sim 129^{\circ}$
C. $\sim 142^{\circ}$
D. $\sim 157^{\circ}$
E. No idea


## Solution

## Answer: B

Justification: A heptagon has 7 corners, thus each internal angle is 900/7 $\approx 129^{\circ}$.

## Polygon Angles XIX

What is the external angle of this regular heptagon?
A. $\sim 37^{\circ}$
B. $\sim 42^{\circ}$
C. $\sim 51^{\circ}$
D. $\sim 62^{\circ}$
E. No idea


## Solution

## Answer: C

Justification: The internal angle and external angle add up to $180^{\circ}$ because they share a straight line.

## Polygon Angles XX

What is the sum of all external angles in this regular heptagon?
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all external angles in a regular heptagon is $7 \times 51.2857 \ldots=360^{\circ}$.

## Polygon Angles XXI

What is the sum of all internal angles in this regular octagon?
A. $540^{\circ}$
B. $720^{\circ}$
C. $900^{\circ}$
D. $1080^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all internal angles in a octagon is the same as six triangles (see picture below).


## Polygon Angles XXII

What is the internal angle of this regular octagon?
A. $90^{\circ}$
B. $110^{\circ}$
C. $120^{\circ}$
D. $135^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: An octagon has 8 corners, thus each internal angle is $1080 / 8=135^{\circ}$.

## Polygon Angles XXIII

What is the external angle of this regular octagon?
A. $20^{\circ}$
B. $30^{\circ}$
C. $45^{\circ}$
D. $60^{\circ}$
E. No idea


## Solution

## Answer: C

Justification: The internal angle and external angle add up to $180^{\circ}$ because they share a straight line..

## Polygon Angles XXIV

What is the sum of all external angles in this regular octagon?
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all external angles in a regular octagon is $8 \times 45=360^{\circ}$.

## Polygon Angles XXV

From what we have seen before, infer the total external angle for ANY convex polygon.
A. $90^{\circ}$
B. $180^{\circ}$
C. $270^{\circ}$
D. $360^{\circ}$
E. No idea


## Solution

## Answer: D

Justification: The sum of all external angles in any convex polygon is $360^{\circ}$, because the angles have to turn all the way around in a circle like fashion to complete the shape.

